Annotated Teacher's Edition

Second Edition

Financial Algebra

ADVANCED ALGEBRA WITH FINANCIAL APPLICATIONS



Robert Gerver | Richard Sgroi





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Financial Algebra, Second Edition, aligns to the Common Core State Standards for Mathematical Content.

The CCSS provides clear and consistent guidelines so students, teachers, administrators, and parents have an awareness of the mathematics proficiencies expected and how to attain them. The standards are designed to be rigorous and relevant to the real world, reflecting the knowledge and skills that students need for future success.

The CCSS Domain and Standard are identified to demonstrate that *Financial Algebra*. Second Edition, addresses at least one, if not several, core standard in each section.

Conceptual Categories

- Number and Quantity
 Modeling
 Geometry

Algebra

- Functions
 Statistics and Probability

A complete correlation of Financial Algebra, Second Edition, to the CCSS for Mathematical Content is available on the community website.

NGL.Cengage.com/FinancialAlgebra

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MATH TOPICS

Bimodal data Percent
Bivariate data Percentage
Causal relationship Percentile
Correlation Percentile rank
Correlation coefficient Percentiles
Cumulative frequency Range
Domain Raw scores

Explanatory, response, lurking variables
Frequency distribution
Independent and dependent variables
Interpolation and extrapolation
Linear regression analysis

Relative cumulative frequency
Relative frequency
Scatter plot
Sigma notation
Skewed data

Linear regression equation Spreadsheets and formulas Mean absolute deviation Standard deviation

Mean deviation Trend

Measures of central tendency – mean, median, mode Variance

Normal curve Z-scores

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MATH TOPICS

Outliers

Antilogarithm Literal equations Arithmetic sequence Logarithm Change-of-base formula Logarithmic equation Common logarithm Logarithmic form Compound interest Natural logarithm Continuous compounding One-to-one property of logarithms Exponential decay Patterns and conjectures **Exponential equations** Power property of logarithms **Exponential form** Recursive and iterative thinking **Exponential** growth Spreadsheets and formulas Limits

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MATH TOPICS

Average daily balance
Cubic equation
Cubic regression equation
Exponential base e
Exponential equations
Linear equations
Linear regression equation
Linear regression equation

Linear equations
Linear equation
Linear regression equation

Spreadsheets and formulas

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MATH TOPICS

MAIII IOI IOO	
Chord	Metric System
Circle	Middle ordinate
Circumference	Projectile motion
Common ratio	Proportions
Conditional probability formula	Quadratic equation
Diameter	Radius
Domain	Ratios
English Standard System	Slope

Exponential decay

Exponential depreciation

Exponential function

Exponential regression

Exponential regression

Geometric progression

Slope intercept form of a linear equation

Spreadsheets and formulas

Square root function

System of linear equations

System of linear, exponential equations

Geometric sequences Two-way tables
Independent events Venn diagrams
Intersection point x-intercept, y-intercept
Linear equations

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MATH TOPICS

MAIII IOI IOO	
Arithmetic sequence	Literal equations
Cusps	Literal expressions
Domain	Piecewise functions
Exponential functions	Percent
Geometric sequence	Spreadsheets and formulas

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Tax Liability

MATH TOPICS

Graphs of functions

Compound inequality	Literal expressions
Compound inequality notation	Percent
Domain	Piecewise function
Inequalities	Slope, intercept form of a linear equation
Interval notation	Spreadsheets and formulas
Linear equation	

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MATH TOPICS

Average Linear regression equation Bar chart Moving average Candlestick chart Percent decrease Converting fractions to percents Percent increase Cubic regression equation Proportion Line graph Quadratic regression equation Linear equations Spreadsheets and formulas

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MATH TOPICS

Axis of symmetry Objective function Parabola Bias Completing the square method Quadratic equation Complex number Quadratic formula Complex roots Random number tables Experimental design Roots of a quadratic equation Roots, zeros of a quadratic equation Hypothesis testing Sampling Imaginary unit Inequality constraints Surveying Leading coefficient System of linear equations Linear equation System of linear, quadratic equations Linear programming **Unbiased estimators** Literal quadratic equation

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MATH TOPICS

Minimum, maximum

Expected value Percent increase **Exponential equation** Percents Histogram Pie charts Literal equations Probability Mean Rational equations Measures of central tendency Spreadsheets

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MATH TOPICS

Addition, subtraction of matrices Matrix Array Matrix multiplication Bar graph Piecewise functions Central angle Ratio Circle graph Scalar Dimensions of a matrix Scalar multiplication Sector Element of a matrix Greatest integer function Spreadsheets and formulas Inequalities Zero matrix Line graph

New to this Edition

The table below lists changes not included in the first edition. New sections are shown in blue font; new math content is listed after the sections in which it appears. Sections marked with * indicate changes for the Tax Code Update.

Chapter 1 Discretionary Expenses

- 1-1 Discretionary and Essential Expenses measures of central tendency, frequency distributions
- ***1-2** Travel Expenses—cumulative and relative frequency, percentiles
- 1-3 Entertainment Expenses—dispersion, normal curve, mean absolute deviation, range, variance, standard deviation, skew, sigma notation, frequency distributions
- **1-4** Vacation Expenses—normal curve, z-scores
- ***1-5** Personal Expenses—linear regression, scatterplots

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- **2-1** Checking Accounts
- 2-2 Reconcile a Bank Statement
- *2-3 Savings Accounts—arithmetic sequences, common difference, finite and infinite sequences, updated interest rates
- **2-4** Explore Compound Interest
- **2-5** Compound Interest Formula
- **2-6** Continuous Compounding—limits of rational functions
- **2-7** Future Value of Investments
- **2-8** Present Value of Investments
- 2-9 The Term of a Single Deposit Account—common logarithm, natural logarithm, antilogarithm, change of base formula, logarithmic equations
- 2-10 The Terms of a Systematic Savings Account systematic savings account, systematic withdrawal account, One-To-One Property, Power Property

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- 3-2 Loans

- *3-3 Student Loans—linear and exponential student loan functions
- *3-4 Loan Calculations and Regression
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 Venn diagrams
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- **9-2** Market Research—unbiased estimators, sampling, types of samples, critiquing experimental design methods

- 9-3 Supply and Demand
- **9-4** Fixed and Variable Expenses
- **9-5** Graphs of Expense and Revenue Functions—completing the square
- 9-6 Breakeven Analysis
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- **10-5** Investment Diversification

Chapter 11 Prepare a Budget

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- **11-2** Electronic Utilities
- 11-3 Charting a Budget
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Chapter 8

The Stock Market

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What do you think Frank Hubbard meant in this quote?

The safe way to double vour money is to fold it over once and put it in your pocket.

-Frank Hubbard, journalist

In the future, you will incur many expenses, such as a home, automobile, insurance, food, clothing, and health care. Some are major expenses and some are minor, but each costs money. To have money for major expenses, it helps to have your savings grow in value. You have already learned how bank interest can help your money grow. However, the prevailing bank interest rates limit the degree to which your money can grow. Investing can help money grow in value, and there is no limit to the amount of growth, but you can also lose all of your investment.

You need to find a personal balance between risk and reward when you make choices about investments. Investments are never without questions. Did you miss the chance to make more money because you were being overly cautious? Was the investment too risky? Did you risk losing principal by investing in something that may not have had a sound foundation?

Investors struggle with these questions every day. The stock market is a forum in which the investment risk/reward balance is put to the test. Will the market advance? Will the market decline? No one can be certain. Will the corporations you choose flourish, grow, and succeed, or falter? With a strong knowledge of the stock market, corporations, and investment strategies, you as an investor can make decisions that are based on experience, data, trends, and mathematics.

"This information is interesting and relevant! Showing real-world relevance is always a good lead into the section."

A relevant quote and chapter **introduction** set the stage for the topics covered in the chapter.

Really?

Gorporations sometimes choose names that are personal, humorous, historical, or psychological. Many are acronyms, where a new word is created by the first letters of several words. Below are some well-known corporations and how their names were established.

Amazon.com was originally known

names were established.
Amazon.com was originally known
as Cadabra.com. Its founder selected
Amazon as a corporate name because the
Amazon River has the largest volume of
any river in the world. He also wanted
a name that began with "A" so that
alphabetically, it would appear at the top
of a list

of a list.

Coca-Cola is a name that has its origins in the ingredients of the product—coca leaves and kola nuts.

The founder, John Pemberton, changed

the "K" in kola to a "C" for appearance

the 'K' in kola to a 'C' for appearance purposes.
Adidas is taken from the name of the company's founder, Adolph (Adi) Dassler.
eBay was created by Pierre Omidyar, who originally wanted to use the name Echo Bay. The name was already taken by a gold mining company, so he shortened it to eBay.

LoJack is a corporation that makes automobile antitheft devices. The name is a humorous adaptation of the word "hijack."

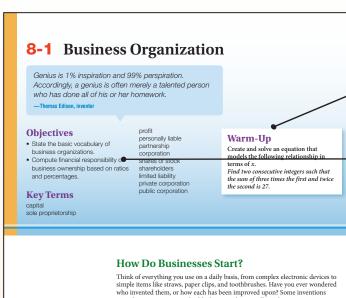
"hijack."
Affac is an acronym for the American
Family Life Assurance Company.
Xerox comes from a Greek
expression for "dry writing." The Xerox
process was invented in 1937 by law
student Chester Carlson.



Really!

Really? Really! captures students' attention by discussing a fascinating real-life topic that relates to the chapter's content.

Structure Puts Math into Context



Warm-Up provides a refresher for basic concepts.

A list of **objectives** provides the main learning outcomes for the chapter.

provide an opportunity to build a business, but not all. It takes imagination, money, and effort to create a successful business. The money used to start or expand a business is called capital.

expand a business is called capital.

A business sowned by one person is a sole proprietorship. The owner, or proprietor, can hire people to help run the business, but these employees are not owners. The owner is responsible for all expenses, including labor and raw materials used in manufacturing a product or providing a service. The money left after all expenses are paid is profit. The owner of a sole proprietorship is entitled

after all expenses are paid is profit. The owner of a sole proprietorship is entitled to all of the profits. However, the owner is responsible, or personally liable, for any losses. Even if the business does not make a profit, the owner must still pay all of the bills of the business.

A business that is owned by a group of people, called partners, is a partnership. Partners share the profits and the responsibility for any losses. The partners are personally liable for any losses. Personal liability may require risking personal property. Sole proprietors and partners must consider this possibility when creating a business.

A corporation is a business organization that can be owned by one person or a group of people. Each owner who invests money in the corporation receives shares of stock in the corporation. The owners are called shareholders. Stock certificates are used as proof of ownership. Unlike sole proprietorships and partnerships, the shareholders in a corporation have limited liability—each

"An intriguing quote at the beginning of each section motivates learning!"

The best way to deal with credit card debt is to educate vourself.

Mark Rosen, Author

"An interesting introduction and a great metaphor for the section!"

Although it's easy to forget sometimes, a share is not a lottery ticket . . . it's part-ownership of a business.

Peter Lynch, American businessman, Investment strategist, and Philanthropist

Nobody ever lost money taking a profit.

Bernard Baruch, Businessman

The Essential Question helps focus attention on the big idea

What are Social Security and Medicare?

How do people gain access to money they keep in the bank?

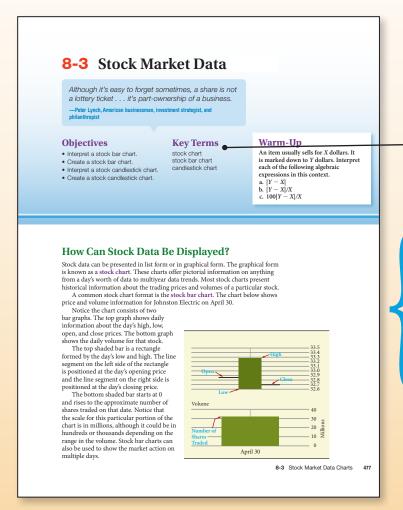
What is compound interest?

What information do you need to know before taking out a loan?

What information does a credit card statement give you?

How do revenue and expenses contribute to profit calculation?

The **Essential Question helps** focus attention on the big idea of each section. You will be able to answer the question by the end of the section.



Each section begins with a discussion of **terms and concepts** related to the section topic.

"This book contains relevant and current information high school students need. The educational focus of today is on standards. This book allows both to be addressed."

When am I ever going to use this in real life?

owner cannot lose more than the value of his or her share of the business. The number of shareholders in a corporation depends on the structure of the business. When all of the shares are owned solely by a few individuals, and are not available for sale to the public, the corporation is a private corporation, also known as a privately held corporation. The New York Yankes are an example of a private corporation. So is Lego, Your local car dealership is most likely a private corporation. When anyone can purchase stock in a corporation, the corporation is a public corporation. You might already be familiar with public corporations such as Nike, McDonald's, Xerox, and Apple. These corporations are owned housewives, doctors, plumbers, teachers, students, senior citizens—anyone who buys a share in the corporation. If a shareholder owns more than 100 for the shares, that shareholder owns a majority of the shares. The puters of shares of stock in public corporations can be found in newspapen on television business channels, and on the Internet.

Skills and **Strategies**

When a business is owned by more than one person, the owners do not necessarily own equivalent portions of the business. Ratios and percentages can be used to represent the financial responsibility of owners and partners. Recall the relationship between decimals and percentages.

To convert a decimal to a percentage, multiply the decimal by 100 and annex a percent sign.

To convert a percentage to a decimal, divide the percent by 100 and drop the percent sign.

EXAMPLE 1

Michelle invests \$15,000 in a partnership that has four other partners. The total investment of all partners is \$240,000. What percent of the business does Michelle own?

SOLUTION Represent Michelle's investment as a fraction of the total investment. Convert the fraction to a decimal and write as a percent.

 $\frac{\text{Michelle's investment}}{\text{Total investment}} = \frac{15,000}{240,000}$

Divide. $15,\!000 \div 240,\!000 = 0.0625$ Multiply by 100. Write a percent sign. $0.0625 \times 100 = 6.25\%$

Michelle owns 6.25% of the partnership.

Kyle invests \$20,000 in a partnership that has five other partners. The total investment of the partners is \$160,000. What percent of the business is owned by the five other partners?

In **Skills and Strategies**, the heart of the section, math concepts are taught through **worked-out examples**. Examples present each math concept step-by-step.

"I love the emphasis on applications with relevance to the world we live in, not on symbolic manipulation."

The total number of shares of stock in Bulls Corp is 650,000. Mike owns 12% of the shares. How many shares of Bulls Corp is 650,000. Mike owns 12% of the shares. How many shares of Bulls Corp stock does he own?

SOUTION Let x represent the number of shares Mike owns.

Express 12% as a fraction. 12% = \frac{12}{100}

Write a proportion. \frac{12}{100} = \frac{650,000}{650,000}

Cross multiply. 100x = (12)(650,000)

Find the product. 100x = 7,800,000

Divide both sides by 100. \frac{100x}{100} = \frac{7,800,000}{100}

Mike owns 78,000 shares of the Bulls Corp.

Check Your other of the stock in a private catering corporation. There are 1,200 shares in the entire corporation. How many shares does Jillian own?

EXAMPLE 3

Three partners are investing a total of \$900,000 to open a garden and landscaping store. Their investments are in the ratio 23:5. How much does the partner that invested the least contribute?

SOUTION Use the ratio 23:5 to write an expression for the amount each partner invested. Let 2x represent the amount invested by the first partner.

Let 3x represent the amount invested by the first partner.

Let 3x represent the amount invested by the first partner.

Let 3x represent the amount invested by the third partner.

Write an equation showing the three investments total \$900,000.

Check Your Two partners are starting a wedding planning business. The total investment is \$45,000. Their investments are in the ratio 4:5. How much does each investor contribute?

The partner that invested the least is represented by the expression 2x. Substitute \$90,000 into the expression. 2(90,000) = 180,000The partner who invested the least amount contributed \$180,000.

10x = 900,000

All math concepts are taught within **real-life context**. When am I ever going to use this in real life? is answered here!

Ongoing Assessment and Review

The trading prices for the first three days are A, B, and C. The average of those

 $\frac{A+B+C}{2} = \frac{A}{2} + \frac{B}{2} + \frac{C}{2}$

Using the method in Example 1, find the average of days 2–4 using B, C, and D. This is the same as subtracting price A and adding price D, or

Rearranging the terms and simplifying, this process is the same as finding the $\,$

$$\frac{A}{3} - \frac{A}{3} + \frac{B}{3} + \frac{C}{3} + \frac{D}{3} = \frac{B}{3} + \frac{C}{3} + \frac{D}{3} = \frac{B+C+D}{3}$$

EXAMPLE 2

Use the subtraction and addition method to determine the 4-day SMA for the following closing prices.

\$121, \$122, \$120, \$119, \$124, \$128, \$126

 $\textbf{SOLUTION} \ \, \text{Calculate the average closing prices of days 1-4}.$

Add the first four prices. Divide by 4. $\frac{121 + 122 + 120 + 119}{120 + 120} = 120.50.$

Use subtraction and addition to determine the averages for days 2–5.

Use previous average, $\frac{121}{4}$, and $\frac{124}{4}$

$$120.50 - \frac{121}{4} + \frac{124}{4} = 121.25$$

Find the averages for days 3-6 and days 4-7.

$$121.25 - \frac{122}{} + \frac{128}{} = 122.75$$

Use previous average, $\frac{120}{4}$, and $\frac{126}{4}$

$$\begin{array}{c}
 4 & 4 \\
 122.75 - \frac{120}{4} + \frac{126}{4} = 124.25
 \end{array}$$

The simple moving averages are \$120.50, \$121.25, \$122.75, and \$124.25.

Use the subtraction and addition method to determine the 3-day SMA for the closing prices \$28, \$31, \$37, \$38, and \$35.

In Example 2, what would the eighth trading day's closing price have to be so that

the next moving average remains the same at \$124.25?

Extend Your

Check Your

Understanding

8-4 Trends in Stock Closing Prices

"I like the immediate check of understanding instead of waiting until the end of the chapter."

Check Your Understanding

allows you to immediately practice the concept on your own. The questions are similar to the example and help you gauge your understanding of the skills being taught.

Applications

Never try to walk across a river just because it has an average depth of four feet.

- Why might the author be warning readers to be cautious of averages? How might these words apply to what you have learned?
 In Exercises 2–5, use the method Illustrated in Example 1 to determine the simple moving averages by repeatedly finding sums.

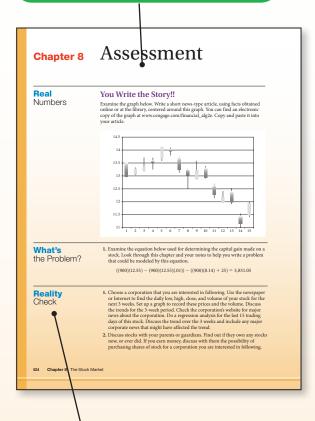
 Determine the 3-day SMA for the 10-consecutive-day closing prices of Anglés Listin. Listed below.
- \$7.78 \$8.08 \$7.99 \$8.02 \$7.89 \$8.72 \$9.19 \$9.16 \$8.98 \$9.38
- 3. Determine the 5-day SMA for the 10-consecutive-day closing prices for Sherwin-Williams Co listed below.

 \$242.50 \$273.98 \$278.16 \$293.94 \$285.04
- \$290.80 \$296.02 \$291.01 \$293.41 \$286.85
- \$290.80 \$290.02 \$291.01 \$293.41 \$288.85 4. Determine the 4-day SMA for the 10-consecutive-day closing prices for Wal-Mart Stores Inc. listed below. \$57.35 \$58.61 \$57.98 \$58.07 \$57.50 \$58.63 \$57.16 \$57.18
- Determine the 6-day SMA for the 12-consecutive-day closing prices for Exxon Mobil Corp listed below.
- \$92.60 \$92.46 \$92.45 \$91.79 \$93.07 \$89.70 \$89.61 \$89.51 \$90.07 \$88.82 \$89.93 \$88.82
- In Exercises 6–9, use the method illustrated in Example 2 to determine moving averages by subtraction and addition.
- Determine the 2-day SMA for the 10-consecutive-day closing prices for Western Digital Corp listed below.
- \$101.96 \$101.80 \$101.50 \$103.07 \$104.94 \$105.12 \$105.66 \$104.76 \$100.56 \$101.31
- Determine the 3-day SMA for the 10-consecutive-day closing prices for Procter & Gamble Co listed below. \$66.21 \$65.90 \$67.05 \$67.03 \$66.80
- \$66.65 \$66.65 \$65.80 \$65.92 \$65.21 Determine the 4-day SMA for the 10-consecutive-trading-day closing prices for Toyota Motor Corp listed below.
 \$121.69 \$122.85 \$120.70 \$123.61 \$123.18
- \$122.03 \$122.82 \$124.14 \$124.92 \$124.06
- Determine the 6-day SMA for the 10-consecutive-trading-day closing prices for SunEdison Inc. listed below.
- \$2.65 \$2.63 \$2.70 \$2.63 \$2.50 \$2.65 \$2.66 \$2.56 \$2.52 \$2.37

Carefully developed, applications at the end of each section require you to apply the concepts to a specific question or scenario.

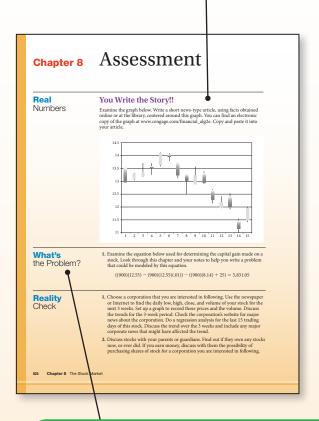
Extend Your Understanding provides an opportunity to solve a more challenging problem.

Chapter Assessment provides an opportunity to check your knowledge of the chapter content.



Reality Check provides specific suggestions for research opportunities, projects, and guest speakers to extend your learning experience.

Real Numbers: You Write the Story! asks you to examine a graph and write a story focused around the graph's information, giving you an opportunity to be creative while at the same time sharpening your graph interpretation skills.



What's The Problem? provides you with a problem posing activity related to a chapter problem. You are given an equation or formula featured in the chapter, with numerical substitutions for each variable. You then have to think backwards and create the problem, using the numbers, that have a solution modeled by the given equation.

"Excellent activities that help connect math to the real world."

Really? Revisited continues the theme of the Really? Really! feature at the beginning of each chapter. In Really? Really! Revisited, you use mathematics to solve a problem or extension related to the Really? Really! theme.



Google is derived from the number googol, which is a 1 with 100 zeros following it. This is equivalent to 10th. Despite the original accidental change in spelling then ton promonation), the name still clicks the idea of something very large. How large is 10th? There isn't a googol of anything on the planet! Lefs take a look at some surprisingly large and surprisingly small numbers. Given that 1,000,000 pennies stacked one on top of another reaches about 1 mile high, how give plennies reach! I mile high, how good pennies reach! I mile high, how good pennies reach. I mile high, how the state of the "power" of exponents, investigate a famous problem in mile than the state of the "power" of exponents, investigate a famous problem in the flow many times would you have to fold a piece of numer so it reached from the state of the power of th

thematics.

How many times would you have to fold a piece of paper so it reached from rth to the Sun, approximately 93 million miles?

- 1. A ream of paper (500 sheets) is 2 inches thick. What is the thickness of one sheet of paper?
- Take a sheet of paper and fold it as many times as you can. For the rest of the problem you will have to imagine that you could continually fold the piece of
- 4. Each fold represents a doubling of the previous thickness, so each fold multiplies the paper thickness by 2°. Use your calculator and trial and error to find the lowest value of x for which the answer exceeds 93 million miles. How many folds would it take to reach to the sun?

many tolds would it take to reach to the sun?

You were probably unable to fold the paper more than six or seven times, so you had to imagine the doubling of the thickness mathematically. After viewing the thickness of the paper after six folds, are you surprised at how few folds it will take the thickness of the paper to reach the sun? The "power" of 2 is smazing!

Applications

- Nick and Matt are partners in a local health food store. They needed \$73,000 to start the business. They invested in the ratio 37, Nick to Matt.
 How much money did each invest?
 What percent of the business was owned by Matt? Round to the nearest tenth of a percent.
- Tom purchased shares of DuPont for \$47.65 per share. He plans to sell the shares when the stock price rises 20%. At what price will he sell his shares?
- 3. The top three shareholders in a certain corporation each own s shares of stock. The corporation's ownership is represented by a total of x shares of stock. Express the percent of the corporation owned by the top three shareholders algebraically.
- Maribel purchased 2,000 shares of stock for \$25.43 per share. She sold them for \$44.10 per share. Express her capital gain to the nearest tenth of a percent.
- 5. A local hairstylist bought 450 shares of a cosmetics corporation for \$33.50 per share. He sold the shares hore \$39.00 per share? He sold the shares hore shared in the price per share? Round to the nearest tenth of a percent.

 b. What was the total purchase price for the 450 shares?
 c. What was the total selling price for the 450 shares?
 d. What was the percent capital gain for the 450 shares? Round to the nearest tenth of a percent.

"I love how it is tied to what started the chapter!"

"Great variety of problems that will prepare students for life outside of school!"

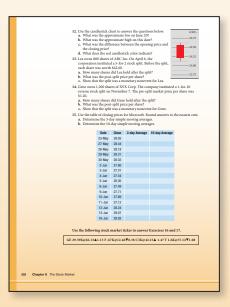
Google is derived from the number googsd, which is a 1 with 100 zeros following it. This is equivalent to 10th. Despite the original accidental change in spelling the rate opposation, the name utilised to the fact of something very large, the result of the special control Really? Really! Revisited Tom purchased shares of DuPont for \$47.65 per share. He plans to sell the shares when the stock price rises 20%. At what price will he sell his shares?

C. While is the special abundancy clear bounds in the nearest center of a A. Whit was the difference between the 25 work high and the 52 work has for uses abused 24 Minest Demount he day's high and he for one share of Sandhard Copper?

C. Which sinch had a close that was further from the day's low?

A. Determine the close was bland; 2 in PloSagua Chau.

C. Which wise had person and the control of the cont | Section | Sect Market Data, As of the Close on March 3



Meaningful applications at the end of each chapter require you to apply concepts that were taught throughout the chapter.

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